

Approximate-Current Instanton Analysis: Detecting Vulnerability in the Power Grid

Jonas Kersulis¹, Dr. Michael Chertkov², Dr. Scott Backhaus², Dr. Ian Hiskens¹ 1. University of Michigan Electrical Engineering: Systems., 2. Los Alamos National Lab Center for Nonlinear Studies

Introduction

Renewable fluctuations add vulnerability to the power grid.

As renewable generation fluctuates about its forecast, power flows and voltage magnitudes throughout the grid undergo complicated shifts. Most variations are harmless, but even a seemingly benign perturbation can violate network constraints.

The instanton is the most likely generation pattern that violates a constraint.

possible generation patterns, some violate network Of all constraints. Of these, the most likely to occur is the instanton.

The nonlinear AC instanton problem has no guaranteed solution.

The accuracy of the AC instanton formulation has a price: the problem is non-convex and may not have a solution. This is unacceptable in a real-time environment.

The linear DC instanton problem has questionable accuracy.

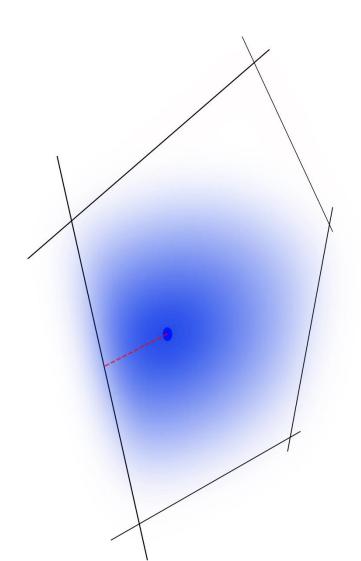
When the DC power flow approximation is applied to the instanton problem, an analytic solution may be found by matrix inversion. Because the instanton lies on a network constraint, however, DC assumptions (like flat voltage profile) are suspect.

Accommodating non-flat voltage profiles improves instanton accuracy.

The new method maintains convexity while accommodating non-flat voltage profiles and reactive power injections.

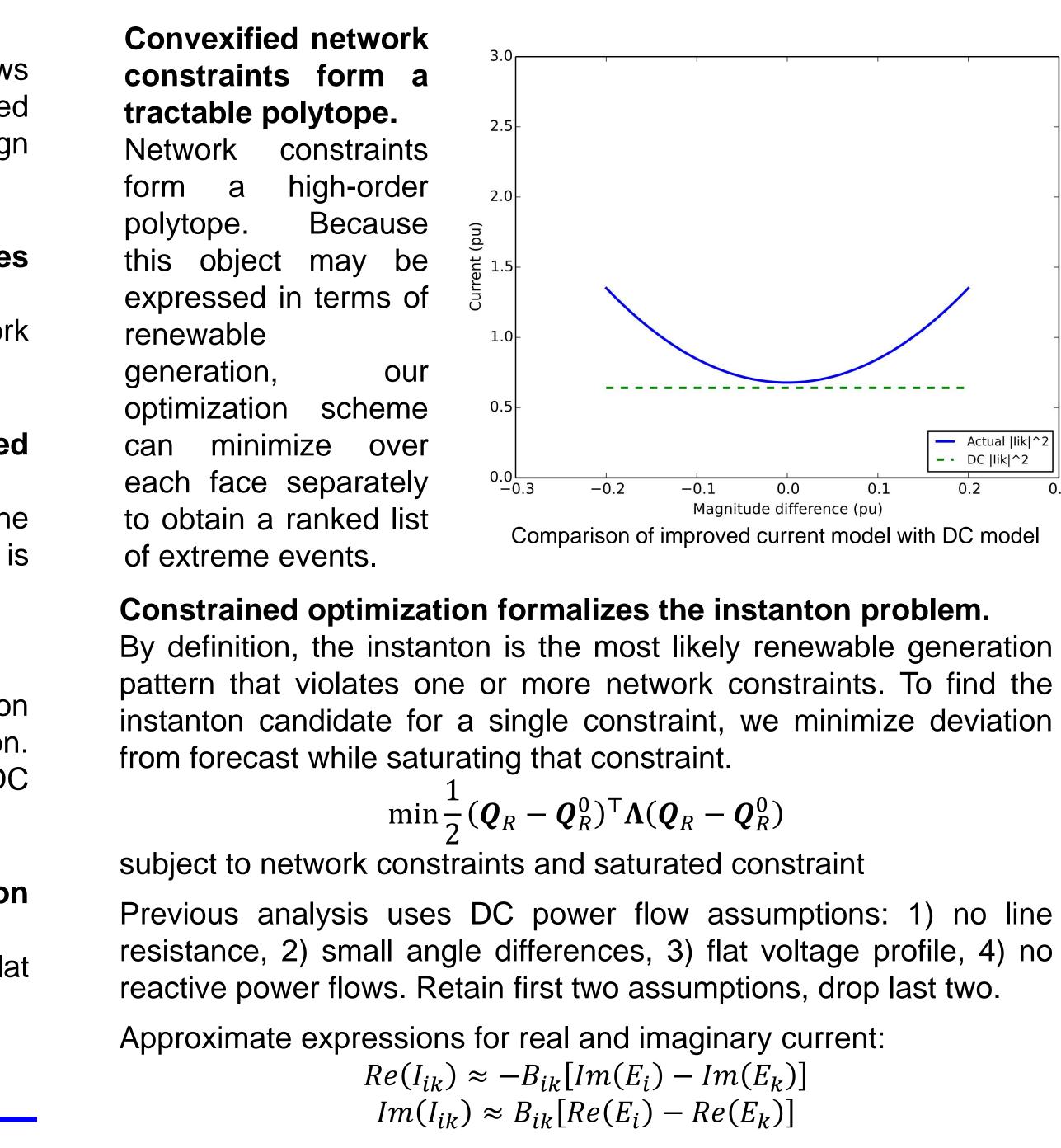
Objectives

- 1. To use approximate AC methods to develop an instanton-finding tool with
 - a) greater accuracy than DC instanton method,
 - b) guaranteed convergence,
 - rapid solution time (subexponential in network size), and
 - d) insightful output (ranked list of extreme events, reconfiguration assistance)
- 2. To characterize differences between DC and approximate AC instanton methods
- 3. To understand differences between DC and approximate AC power flow methods



Two-dimensional depiction of instanton search. Starting from the forecast (dot), the dashed line shows the most likely shift in generation that would violate a constraint (solid line).

New Method: Current Constraint



Square each term to obtain approximate current magnitude: $|I_{ik}|^2 \approx B_{ik} \left(V_i^2 + V_k^2 - 2V_i V_k \cos \theta_{ik} \right)$

Solve for angle:

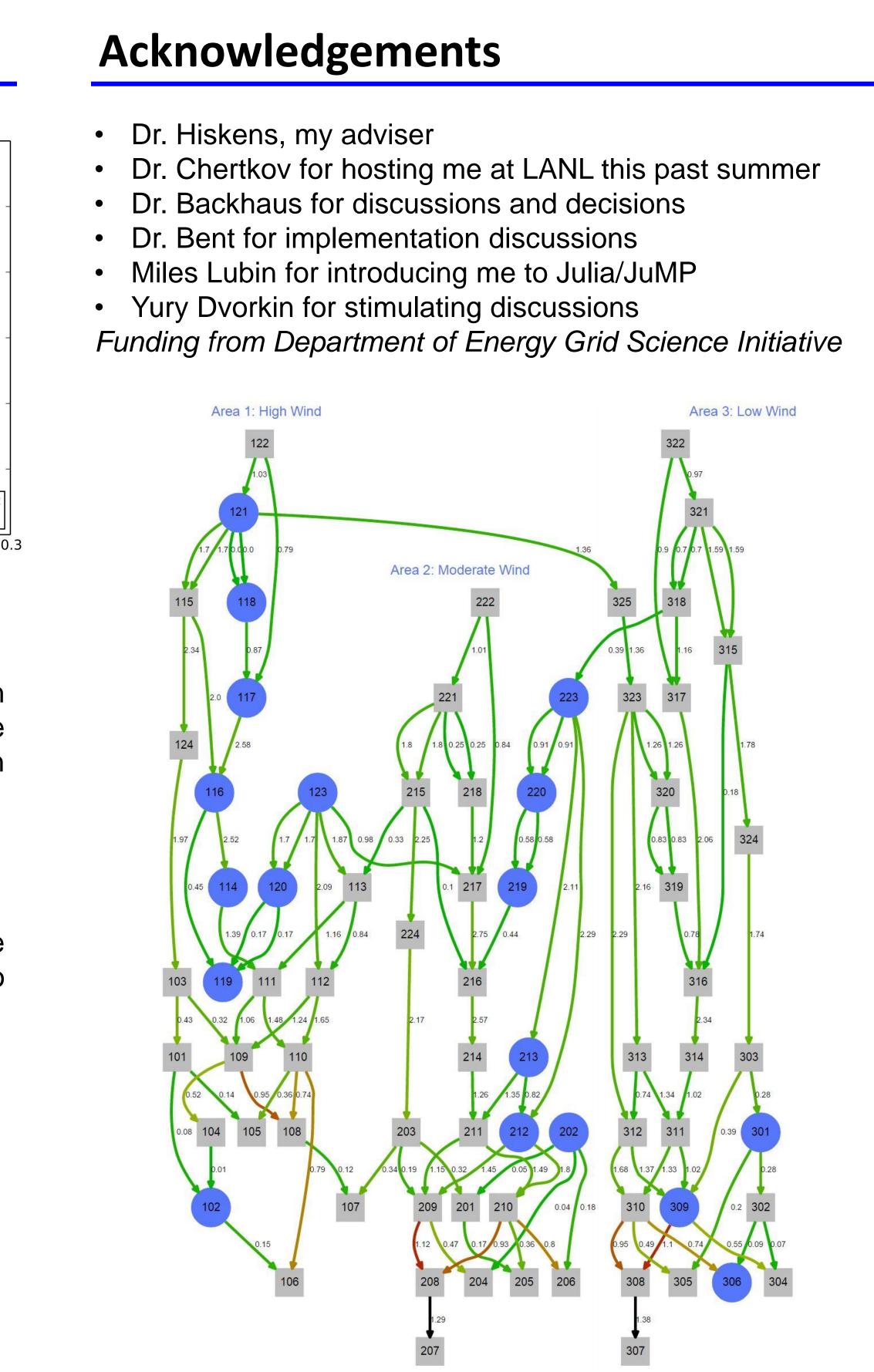
$$\theta_{ik} = \cos^{-1} \left(\frac{V_i^2 + V_k^2 - \left(|I_{ik}^{lim}| x_{ik} \right)^2}{2V_i V_k} \right)$$

Compare with DC constraint: $\theta_{ik} = x_{ik} P_{ik}^{\lim}$

Any line with significant voltage difference is more vulnerable than DC instanton analysis says.

PQ decoupling means we can pre-compute voltage magnitudes from reactive injections. (If voltages were not fixed, we would need to approximate cosine.)





Implementation on IEEE RTS-96 Network

References

[1] Baghsorkhi, S.S., and I.A. Hiskens. "Analysis Tools for Assessing the Impact of Wind Power on Weak Grids," 1–8, 2012.

[2] Coffrin, Carleton, and Pascal Van Hentenryck. "A Linear-Programming Approximation of AC Power Flows," unpublished.

[3] Coffrin, Carleton, P. Van Hentenryck, and R. Bent. "Approximating Line Losses and Apparent Power in AC Power Flow Linearizations." In 2012 IEEE Power and Energy Society General Meeting, 1-8, 2012.